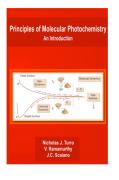
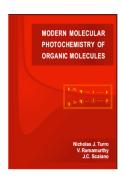
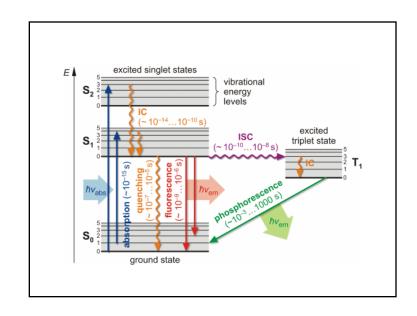
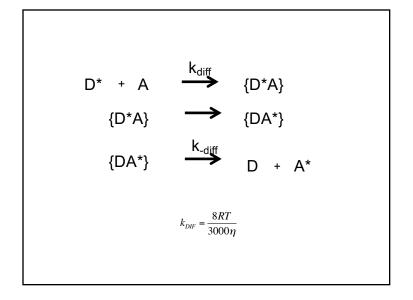
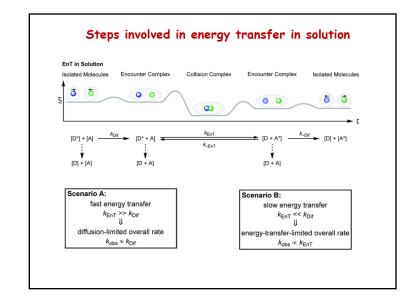
Electron and Energy Transfer Chapter 7 (pp.383-481)











Diffusion

$$k_{DIF} = \frac{8RT}{3000\eta}$$

 η is the viscosity of the solvent (in units of Poise, P) $\it R$ is the gas constant (8.31 x $10^7\,erg/mol$ or 1.99 cal mol $^{-1}$ K $^{-1}$).

For typical non-viscous organic solvents (benzene, acetonitrile, hexane) at room temperature η is ~ 1-10 cP

 $k_{\rm DIF}$ has a value of around 10^9 - 10^{10} M⁻¹s⁻¹.

Possibilities

$$^{1}D^{*} + A \longrightarrow D + ^{1}A^{*}$$

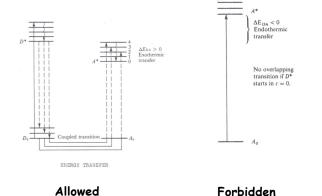
$$1D^* + A \rightarrow D + 3A^*$$

$$-3D* + A \rightarrow D + 1A*$$

$$^3D^* + A \longrightarrow D + ^3A^*$$

Energy Requirement

ED > EA



 $E_D < E_A$

Mechanisms

- · Radiative Energy Transfer
 - Trivial ET
- · Non-Radiative Energy Transfer
 - · Resonance ET
 - Exchange ET

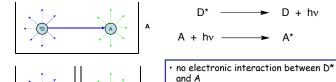
Trivial Energy Transfer

$$^*D \longrightarrow D + hv$$
 $hv + A \longrightarrow ^*A$

Depends On:

- The quantum yield (Φ_e^D) of emission of *D
- \bullet The number of A molecules (concentration) in the path of photons emitted by *D
- The light absorbing ability (extinction coefficient, ϵ_A) of A
- The overlap of the emission spectrum of *D and the absorption spectrum of A, with consideration given to the extinction coefficient, ε_A, of A at the wavelength of overlap.

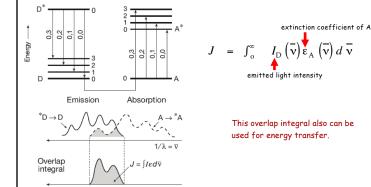
Trivial energy transfer (radiative energy transfer)



• D* emits a quantum of light which is absorbed by A

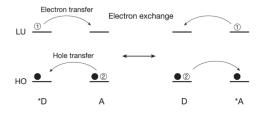
A physical encounter between A and D^{\star} is not required, the photon must only be emitted in an appropriate direction and the medium must be transparent in order to allow transmission.

Criteria for Trivial Energy Transfer: Spectral Overlap

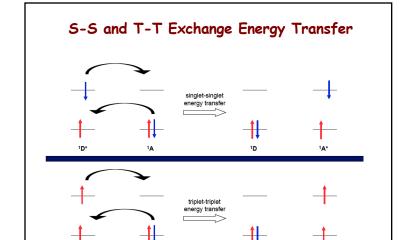


Non-Radiative Energy Transfer

Exchange Energy Transfer
Dexter Energy Transfer
Collisional Energy Transfer



 k_{ET} (exchange) = $KJ \exp(-2 r_{\text{DA}}/L)$



Criteria for Exchange Energy Transfer

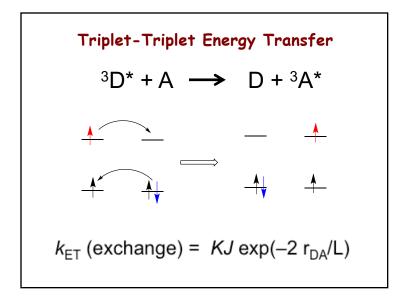
$$k_{\rm ET}$$
 (exchange) = KJ exp($-2r_{\rm DA}/L$)

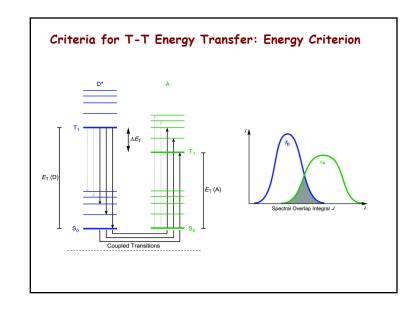
- Spin
- Energy matching
- Distance
- · Orientation

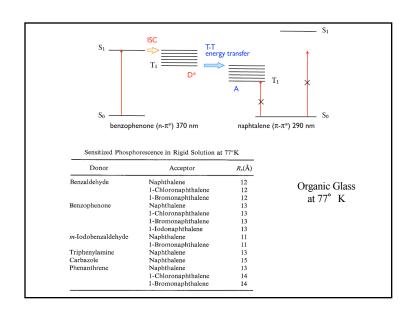
where K is related to the specific orbital interactions such as the dependence of orbital overlap to the instantaneous orientations of *D and A.

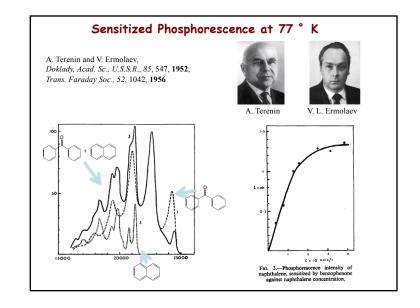
 ${\cal J}$ is the normalized spectral overlap integral, where normalized means that both the emission intensity (${\cal I}_D$) and extinction coefficient (ϵ_A) have been adjusted to unit area on the wavenumber scale. It is important that ${\cal J}_r$, by being normalized does not depend on the actual magnitude of ϵ_A .

 r_{DA} is the donor-acceptor separation relative to their van der Waals radii, L

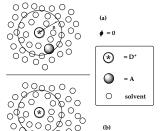








Energy Transfer in the Absence of Diffusion The Perrin Formulation of Quenching. The Quenching Sphere



There exists a volume in space, termed a "quenching sphere", about *D whose radius is R; if a quencher molecule, A, is within this quenching sphere, then *D is deactivated with 100% efficiency.

If A molecule is outside of the quenching sphere, it does not quench *D at all.

According to the Perrin model, the measured lifetime of *D molecules that are not in the quenching sphere will be the same as the lifetime for *D in the absence of A.

A bit of history: Glass at 77° K to Solution at RT

Sensitized phosphorescence of aromatic compounds A. N. Terenin and V. Ermolaev, *Doklady, Acad. Sc., U.S.S.R., 85*, 547, **1952**

Sensitized phosphorescence in organic solutions at low temperature: Energy transfer between triplet states

A. N. Terenin and V. Ermolaev, Trans. Faraday Soc., 52, 1042, 1956

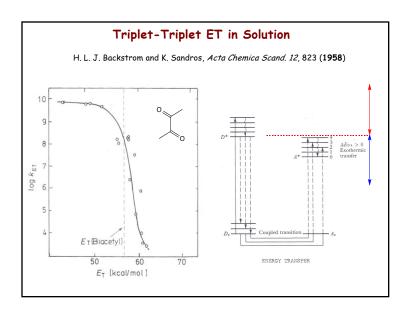
Quenching of biacetyl fluorescence in solution
H. L. J. Backstrom and K. Sandros, *J. Chem. Phys.* **1955**, 2197

The quenching of long-lived fluorescence of biacetyl in solution H. L. J. Backstrom and K. Sandros, *Acta Chemica Scand.* **1958**, *12*, 823

Transfer of triplet state energy in fluid solution: Sensitized Phopshorescence and its application to the determination of triplet state lifetimes

H. L. J. Backstrom and K. Sandros, Acta Chemica Scand. 1960, 14, 48

Energy transfer from the triplet state G. Porter and F. Wilkinson, *Proc. Royal Soc. A*, **1961**, *264*, 1



Triplet-Triplet ET in Solution Correlation of rate with triplet energy gap

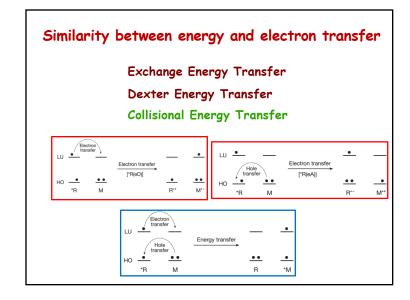
G. Porter and F. Wilkinson, Proc. Royal Soc. A, 264, 1 (1961)

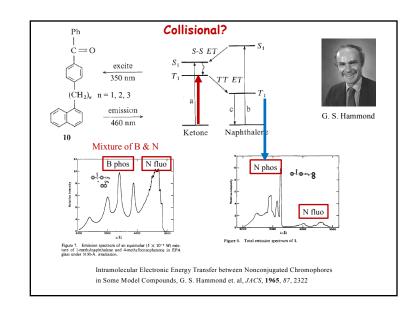


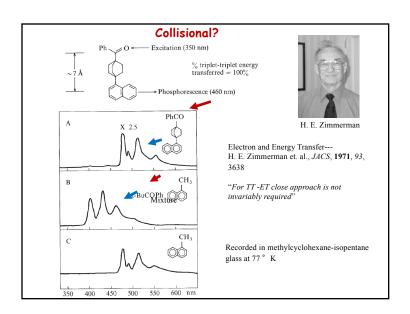
G. Porte

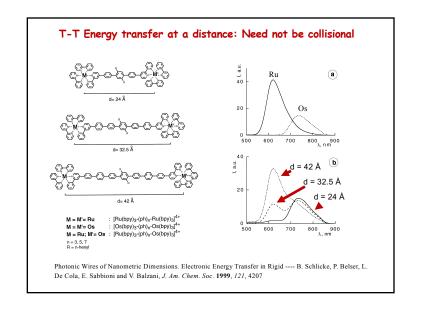
TABLE 6.5. Rate Constants for Triplet-Triplet Energy Transfer (56)

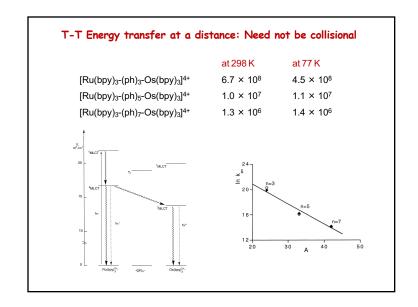
Donor	Acceptor	Solvent	ΔE_t , kcal/mole	M^{-1} sec ⁻¹
Triphenylene	Naphthalene	Hexane	6,30	$1.3 \pm 0.8 \times 10^{8}$
Phenanthrene	1-Iodonaphthalene	Hexane	3.15	$7 \pm 2 \times 10^{8}$
Phenanthrene	1-Iodonaphthalene	Ethylene glycol	3.15	$2.1 \pm 0.2 \times 10^{6}$
Phenanthrene	1-Bromonaphthalene	Hexane	2.57	$1.5 \pm 0.8 \times 10^{8}$
Naphthalene	1-Iodonaphthalene	Ethylene glycol	2.29	$2.8 \pm 0.3 \times 10^{8}$
Phenanthrene	Naphthalene	Hexane	0.86	$2.9 \pm 0.7 \times 10^{6}$
Naphthalene	Phenanthrene	Hexane	-0.86	<2 × 104
Naphthalene	Benzophenone	Benzene	-8.90	$\leq 1 \times 10^4$

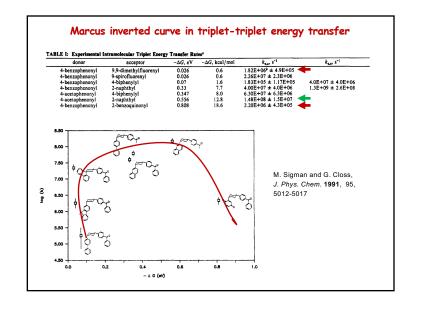


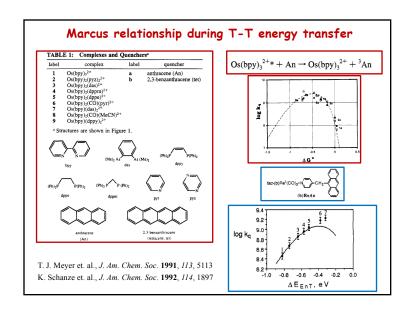


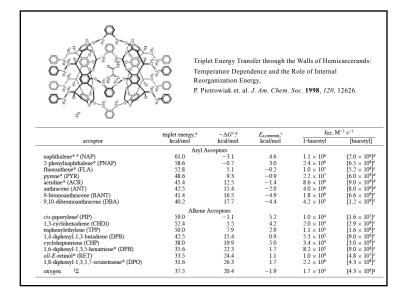


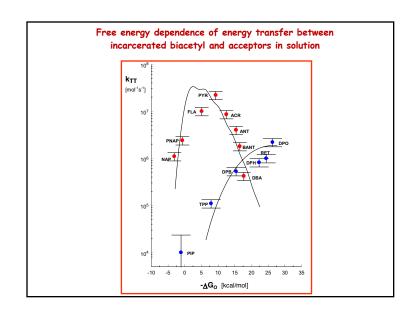








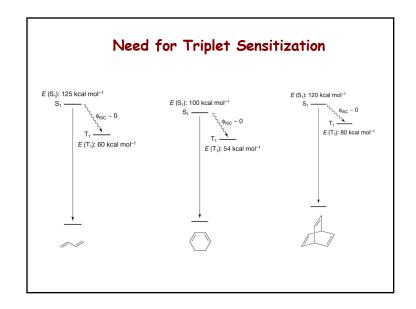


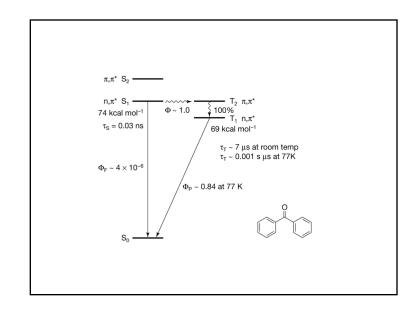


Value of triplet-triplet energy transfer in organic photochemistry

Sensitizers: Generation of reactive triplets

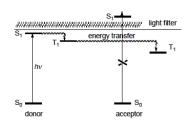
Quenchers: Identification of reactive triplet

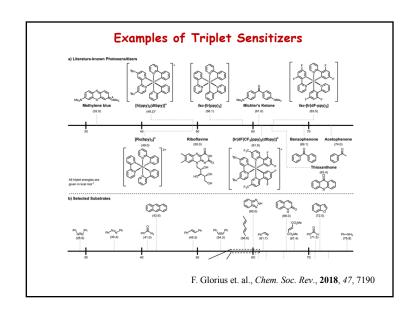




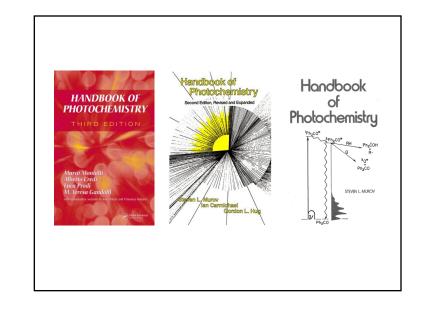
Sensitizers

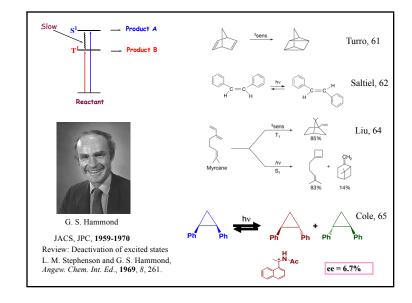
- > Should be able to excite the sensitizer alone even in presence of acceptor.
- \succ Sensitizer should have high intersystem crossing efficiency (S₁ to T₁).
- > Sensitizer should have triplet energy higher than the acceptor.
- > Sensitizer should be photostable.

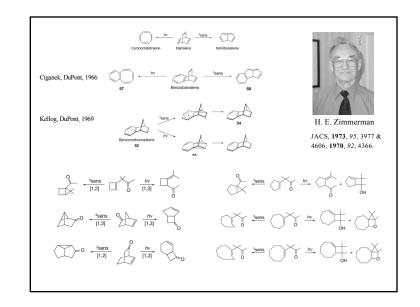


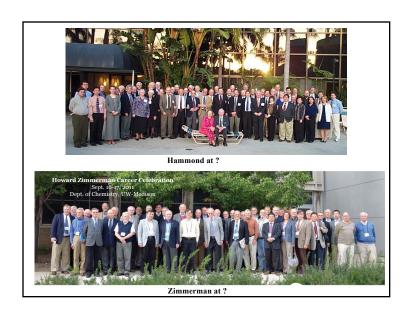


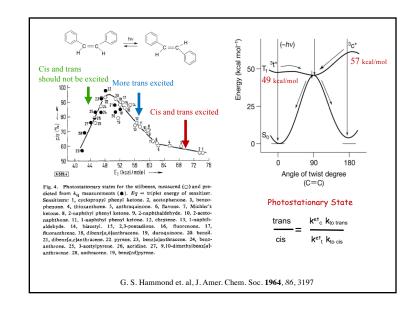
	$E_{\rm S}$	E_{T}	$ au_{ m S}$	$ au_{ m T}$		
Compound	(kcal r	nol ⁻¹)	(s)		Conf. T_1	Φ_{ST}
Benzene	110	84	$\sim 10^{-7}$	10^{-6}	π,π^*	0.2
Acetone	~ 85	~ 78	10^{-9}	10^{-5}	n,π^*	1.0
Xanthone		74			π,π^*	1.0
Acetophenone	~ 79	74	10^{-10}	10^{-4}	n, π^*	1.0
4-CF ₃ Acetophenone		71			n,π*	1.0
Benzophenone	~ 75	69	10^{-11}	10^{-4}	n,π*	1.0
Triphenylene	83	67	$\sim 5 \times 10^{-8}$	10^{-4}	π,π^*	0.9
Thioxanthone	78	~ 65				
Anthraquinone		62			n,π^*	1.0
4-Ph-benzophenone	77	61		10^{-4}	π,π^*	1.0
Michler's ketone		61				1.0
Napthalene	92	61	10^{-7}	10^{-4}	π,π^*	0.7
2-Acetonaphthalene	78	59		10^{-4}	π,π^*	1.0
1-Acetonaphthalene	76	57		10^{-4}	π,π^*	1.0
Chrysene	79	57	5×10^{-8}		π,π^*	0.8
Biacetyl	~ 60	55	10^{-8}	10^{-3}	n, π^*	1.0
Benzil	~ 59	54	$\sim 10^{-8}$	10^{-4}	n,π*	1.0
Camphorquinone	~ 55	50	$\sim 10^{-8}$		n,π*	1.0
Pyrene	77	49	$\sim 10^{-6}$		π,π^*	0.3
Anthracene	76	47	$\sim 5 \times 10^{-9}$	10^{-4}	π,π^*	0.7
9,10-Dichloroanthracene	~ 74	40	$\sim 5 \times 10^{-9}$	10^{-4}	π,π^*	0.5
Perylene	66	~ 35	5×10^{-9}		π,π^*	0.005

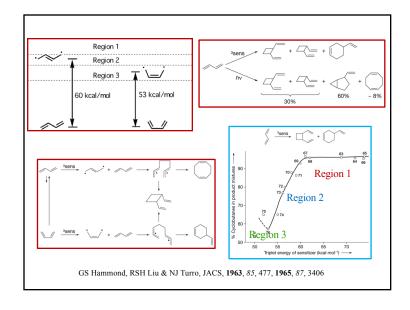


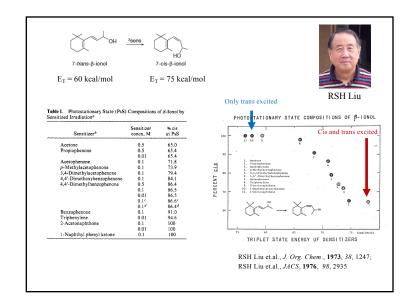


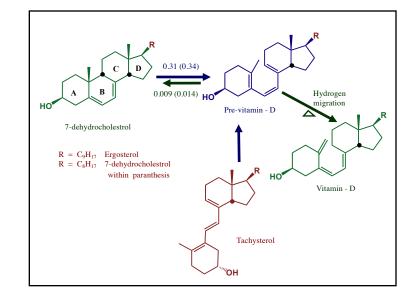


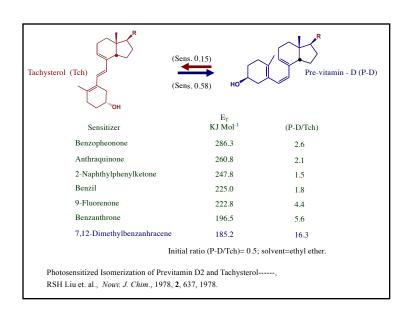


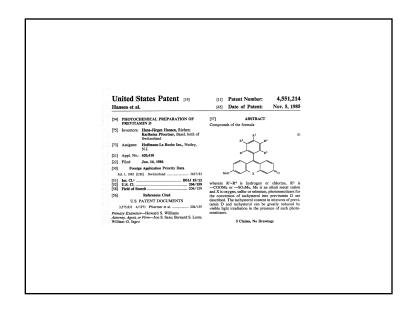


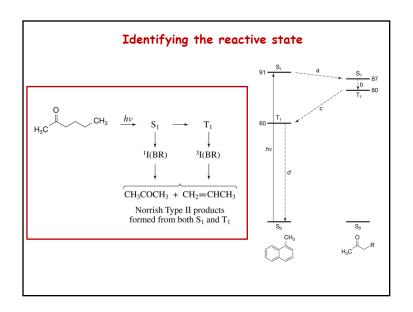


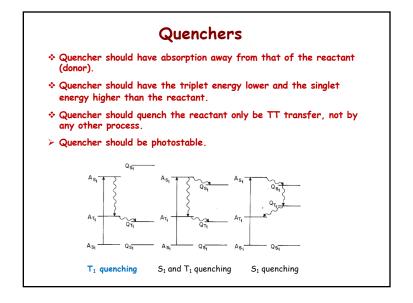


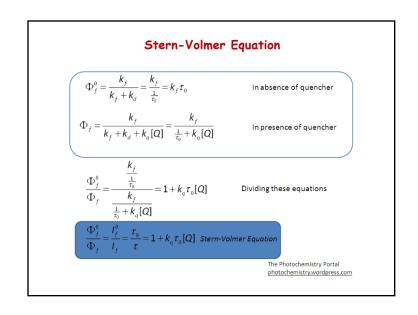


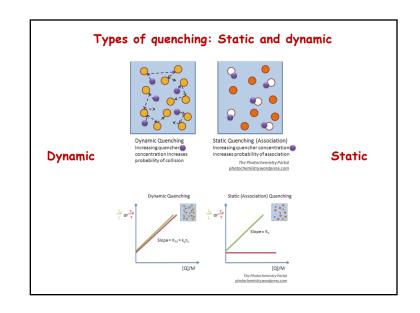


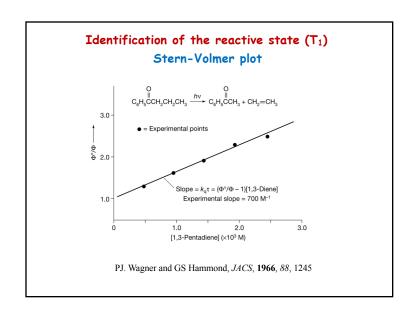


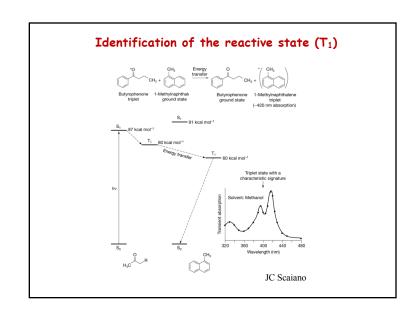


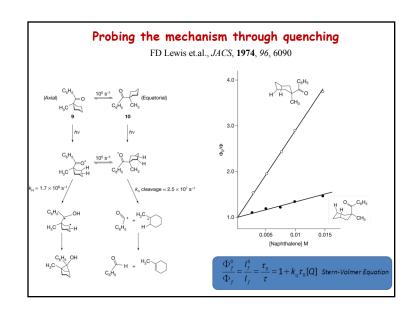


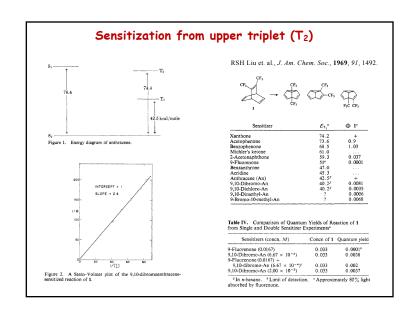


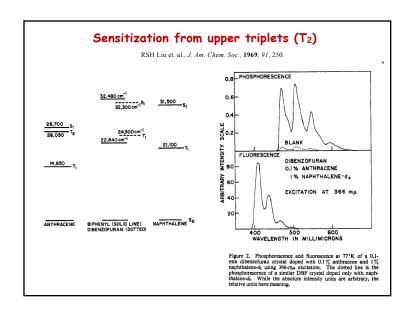


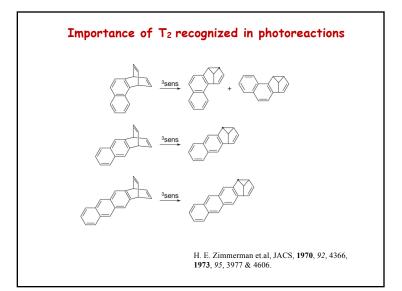












References

Deactivation of excited states, L. M. Stephenson and G. S. Hammond, *Angew. Chem. Int. Ed.*, **1969**, *8*, 261.

Energy Transfer and Organic Photocehmistry, A. Lamola & N. J. Turro, Wiley, 1969

Dual catalysis strategies in photochemical synthesis, T. P. Yoon et.al., *Chem. Rev.*, **2016**, *116*, 10011

Energy transfer catalysis mediated by visible light: Principles, applications and directions, F. Glorius et. al., *Chem. Soc. Rev.*, **2018**, *47*, 7190

Visible-light induced organic photochemical reactions through energy transfer pathways, Q-Q. Zhou----W-J. Xiao, *Angew. Chem. Int. Ed.*, **2019**, 58, 1586.

Delayed Fluorescence

Triplet—Triplet Annihilation

Up-conversion

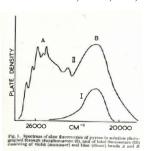
Triplet Fusion

Antistokes delayed fluorescence

Sensitized antistokes delayed fluorescence

Beginnings of Delayed Fluorescence

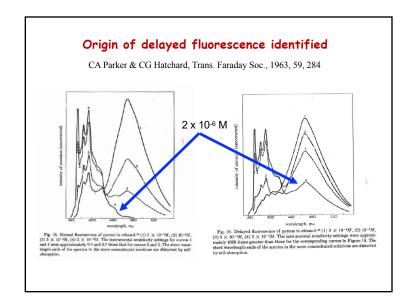
B. Stevens & E. Hutton, Nature, 1960, 186, 1046



Lifetime: $1.8 \pm 0.2 \text{ ms}$ Origin unclear

Ratio of Band Intensities of Dimer and Monomer for Normal and Delayed Fluorescence**

Concentration of pyrene, c	Ratio for normal fluorescence, ϕ_D/ϕ_M	$K_1 = \phi_D/\phi_M c$	Ratio for delayed fluorescence, $\theta_{\rm D}/\theta_{\rm M}$	$K_3 = (\theta_D/\theta_M - K_2)/c$
$3 \times 10^{-3}M$	5.20	1.73×10^{3} liter mole ⁻¹	9.35	2.88×10^{3} liter mole ⁻¹
10-3	1.80	1.80	4.18	3.47
3×10^{-4}	0.514	1.71	1.69	3.28
10-4	0.157	1.57	0.970	2.64
2×10^{-5}	0.031	(1.5)	0.777	3.55
2×10^{-6}	-	_	0.706 (= K_2)	-



Delayed Fluorescence

Anthracene, Phenanthrene, Naphthalene, Benzpyrene etc.

CA Parker & CG Hatchard, Proc. Chem. Soc., 1962, 147

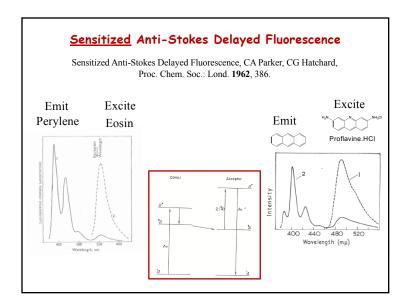
CA Parker & CG Hatchard, Proc. R. Soc. London. Ser.A. 1962, 269, 574

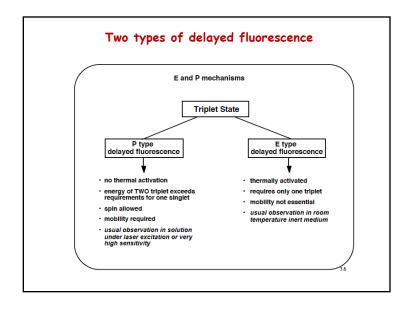
CA Parker & CG Hatchard, Nature, 1963, 200, 331

"The intensity of the emission is proportional to the square of the rate of light absorption."

Pyrene CA Parker & CG Hatchard, Trans. Faraday Soc., 1963, 59, 284

"The delayed fluorescence produced by triplet-triplet quenching is sharply different from that form eosin. To facilitate distinction between the two types we suggest the one be called E-type (esoin) and the other P-type (pyrene)."

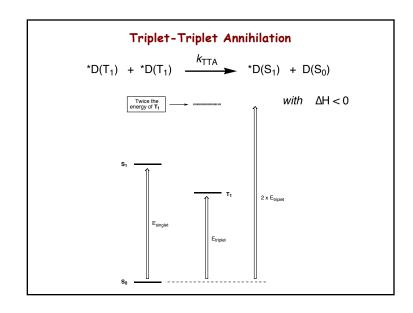


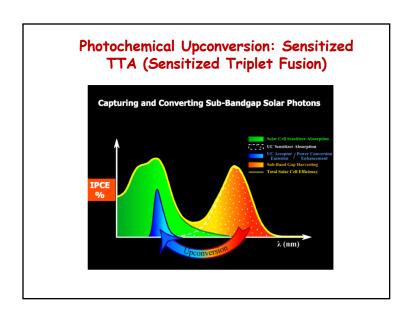


P-type delayed fluorescence

The process in which the first excited singlet state is populated by interaction of two molecules in the triplet state (triplet-triplet annihilation) thus producing one molecule in the excited singlet state

In this biphotonic process the lifetime of delayed fluorescence is half the value of the concomitant phosphorescence.





Not every collision leads to energy transfer

Spin statistics for the interactions of two triplets

			Total spin	Arrow	Multipilicity	Name of final
	T _n	T _{n.}	$S = T_n + T_n$	notation	=(2S+1)	state, Symbol
Case 1	T ₊₁ (↑↑)	$T_{-1}(\downarrow\downarrow)$	0	↑↓↑↓	1	Singlet, S
Case 2	T ₊₁ (↑↑)	$T_0(\downarrow\uparrow)$	+1	↑↑↓↑	3	Triplet, T
Case 3	T ₊₁ (↑↑)	$T_{+1}(\uparrow\uparrow)$	+2	1111	5	Quintet, Q

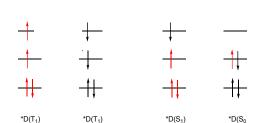
Exchange Energy Transfer

$$^*D(T_1) + ^*D(T_1) \xrightarrow{k_{TTA}} ^*D(S_1) + D(S_0)$$

with $\Delta H < 0$

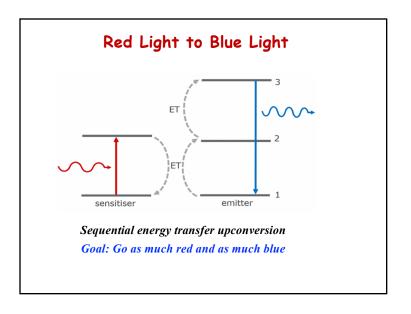
ıl state	

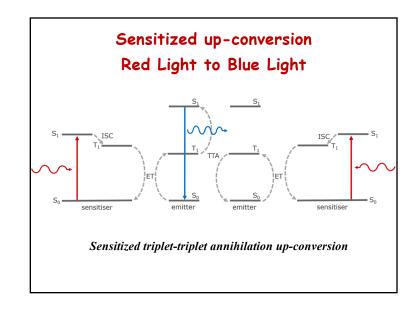
Final states

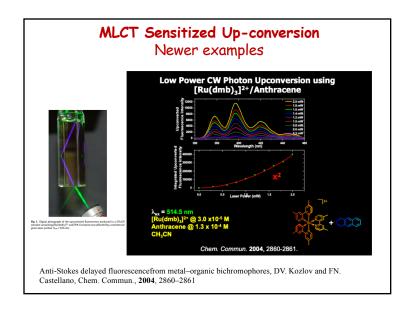


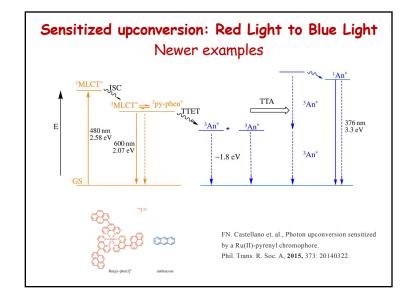
Properties of TTA in Solution Direct light absorption

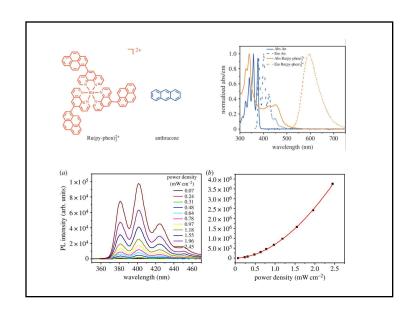
- The rate constants for TTA, ktta, are generally very large.
- With laser light excitation, triplet state concentrations in excess of 10^{-5} M can be readily achieved. Typical products $k_{TTA}[D^*(T_1)]$ may then be around or over 10^5 s⁻¹. Thus, any triplet with lifetime of a few microseconds (a common situation) will undergo at least some TTA in fluid solution.
- The high sensitivity with which fluorescence can be detected makes TTA
 an easily observable process even when it is not the major mechanism for
 triplet decay.

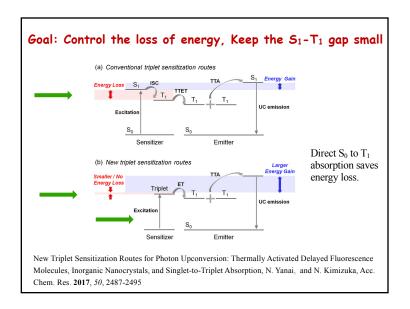


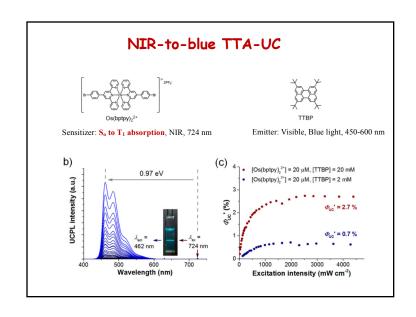


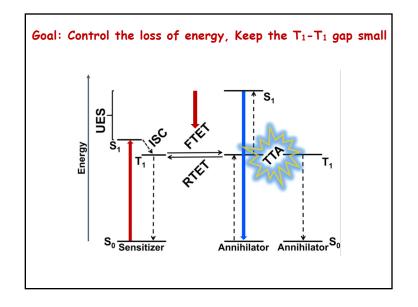


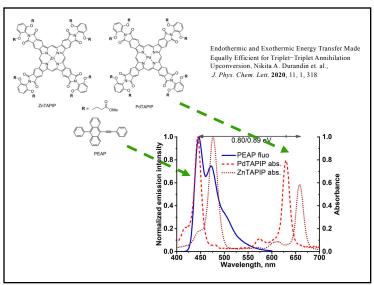


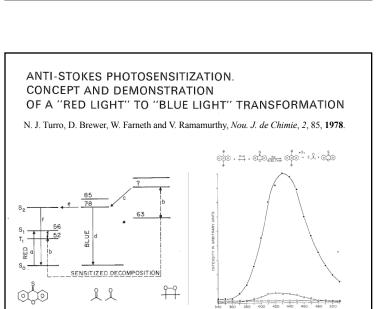


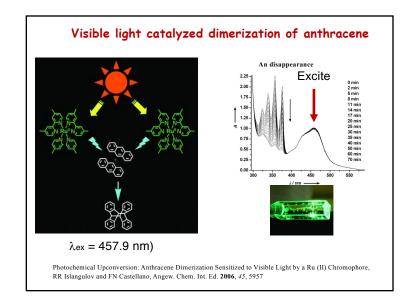












Selected Reviews

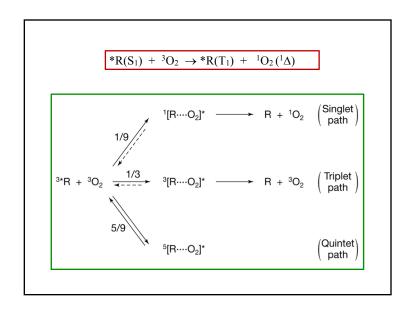
C. A. Parker, Phosphorescence and Delayed Fluorescence from Solutions, Adv. Photochem., **1964**, *2*, 305

Photon upconversion based on sensitized triplet–triplet annihilation, T. N. Singh-Rachford, F. N. Castellano, Coordination Chemistry Reviews, **2010**, *254*, 2560–2573

C. E. McCusker, F. N. Castellano, Materials Integrating Photochemical Upconversion, Top Curr Chem (Z) **2016**, 374, 19

Upconversion Luminescent Materials: Advances and Applications J. Zhou, Q. Liu, W. Feng, Y. Sun, and F. Li, Chem. Rev. **2015**, *115*, 395

New perspectives for triplet–triplet annihilation based photon upconversion using all-organic energy donor & acceptor chromophores, A. Jean-Luc Ayitou et. al., Chem. Commun., **2018**, *54*, 5809.



Representative rate constants and singlet oxygen efficiencies for the quenching of <u>excited singlets</u> by oxygen in acetonitrile at room temperature

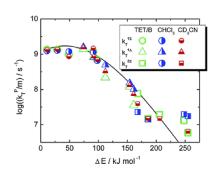
Substrate	Solvent	(S∆S)a	k_q^S , 10^9 (M-1s-1)
Naphthalene	Acetonitrile	≤ 0.09	31
Phenanthrene	Acetonitrile	0	33
Triphenylene	Acetonitrile	≤ 0.02	37
Pyrene	Acetonitrile	0.30	29
Fluoranthene	Acetonitrile	0.30	6.6
Perylene	Acetonitrile	0.27	38
Tetracene	Acetonitrile	0.25	42
Anthracene	Acetonitrile	≤ 0.02	30

For the ET to be effective the singlet-triplet $(S_1 - T_1)$ energy gap of the donor must be greater than the energy gap between the ground and singlet state of oxygen (22.4 kcal/mol), the acceptor.

The π,π^* triplet states of polynuclear aromatics are generally highly efficient at producing singlet oxygen, frequently with $S\Delta \geq 0.8$. The n,π^* triplet states of ketones have low values of $S\Delta$, for example for benzophenone $S\Delta$ is in the 0.3-0.4 range. Depends on the S_1 - T_1 gap.

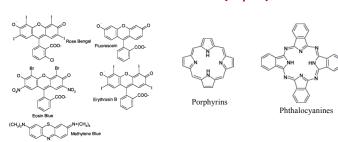
Energy Gap Law for Electronic Energy Transfer to O2

R. Schmidt, J. Phys. Chem. A 2006, 110, 8, 2622



<u>Marcus</u> type relationship. Larger the excess energy (more than needed to generate singlet oxygen) slower the rate constant.

Common 1O2 sensitizers (triplet)



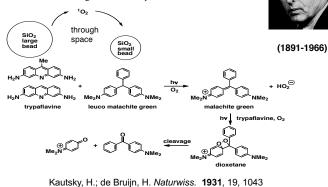
A Compilation of Singlet Oxygen Yields from Biologically Relevant Molecules, R.W. Redmond and J.N. Gamlin, Photochemistry and Photobiology, **1999**, *70*, 391.

Photosensitized singlet oxygen and its applications, MC. DeRosa, RJ. Crutchley, Coordination Chemistry Reviews, **2002**, 233/234, 351.

Physical Mechanisms of Generation and Deactivation of Singlet Oxygen, C. Schweitzer and R. Schmidt, Chem. Rev. **2003**, *103*, 1685.

Hans Kautsky

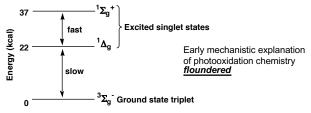
- 1931, brilliant experiments
- Dye and acceptor adsorbed on SiO2 gel beads
- · Oxidation of acceptor
- Suggested: diffusible ${}^{1}O_{2}\left({}^{1}\Sigma_{g}{}^{+}\right)$
- Found himself challenged on this interpretation



History of Research on Singlet Oxygen

- · 19th Century
- 1800s biologists discover: Dyes, oxygen, and light toxic to organisms

Spin state property of O₂



Mulliken, R. S. Nature 1928, 122, 505; Rev. Mod. Phys. 1932, 4, 54

Contemporary skepticism: Hans Gaffron



(1902-1979)

NH NN

N HN

Or

Mg

HO₂C

CO₂H

hematoporphyrin

Chlorophyll a, R=CH₃

Chlorophyll b, R=CHO

+ H₂N H S allyl thiourea (acceptor)

hy (820 nm) acceptor

•Argued the ${}^{1}\Sigma_{g}{}^{+}$ state (37 kcal/mol) could not form by energy

transfer from a dye emitting at 820 nm (35 kcal/mol)

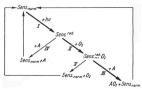
Gaffron, H. Ber. 1935, 68B, 1409; Biochem. Z. 1936, 287, 130

Contemporary Skepticism GO Schenck

1940-1963

Sens--OO (moloxide)

Papers on photooxidation were one-sided Photooxidation attributed to sensitizer—oxygen adduct Many discounted the contribution of 1O_2 ($^1\Delta_q$)



Schenck, G. O. Naturwiss, 1948, 35, 28

References:

Blum, H. F. *Physiol. Rev.* **1945**, *25*, 483 Bowen, E. J. *Discussions Faraday Soc.* **1953**, *14*, 143 Terenin, A. N. *Akad. Nauk S.S.S.R.* **1955**, 85

Livingston, R. S. Conf. Biol. Antioxidants Trans. 1950, 5, 17

G. O. Schenck (1913-2003)

Singlet Oxygen

 $^{1}\Sigma_{g}^{+}$ Singlet Oxygen as the reactive species

H. Kautsky et al., Naturwissenschaften, 1931, 19,1043

H.Kautsky, et. al., Dtsch. Chem. Ges., **1933**, 66, 1588. H. Kautsky, Biochem. Z, **1937**, 291,271(1937)

H. Kautsky, Trans. Faraday Soc., 1939, 35, 216.





3, , , , ,

H. Kautsky

utsky G. O. Schenck

Sens--OO (moloxide)

GO. Schenck, G. O. Naturwiss. 1948, 35, 28

Singlet Oxygen

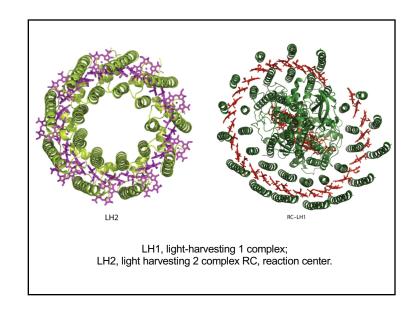
Foote, C. S.; Wexler, S. J. Am. Chem. Soc. **1964**, *86*, 3879 Foote, C. S.; Wexler, S. J. Am. Chem. Soc. **1964**, *86*, 3880 S Wolf, CS Foote, J Rebek Jr. J. Am. Chem. Soc. **1978**, *100*, 7770

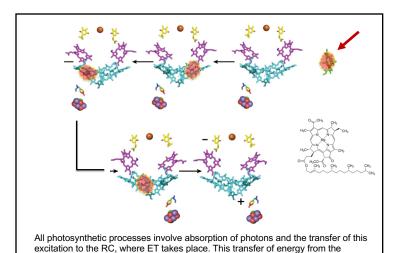


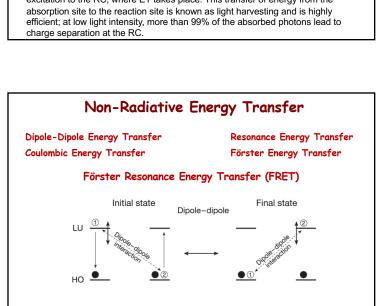
C. S. Foote



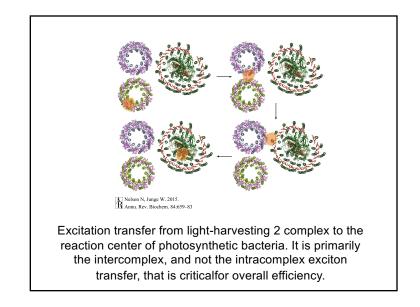
Plants that commonly grow in the shade benefit from having a variety of light-absorbing pigments. Each pigment can absorb different wavelengths of light, which allows the plant to absorb any light that passes through the taller trees.

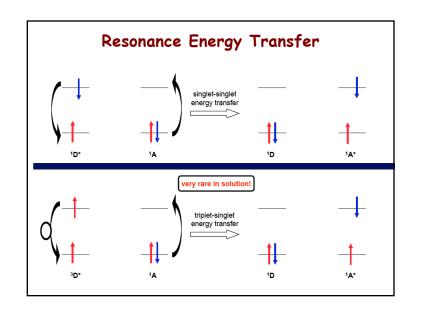


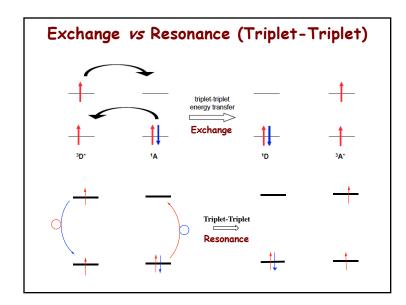




 $k_{\text{ET}} \left(\text{total} \right) \propto \left[\alpha \left\langle \Psi(D^*) \Psi(A) \right| H_{d-d} \left| \Psi(D) \Psi(A^*) \right\rangle^2 \right]$







$\label{eq:milestones} \mbox{Milestones in the Theory of Resonance Energy Transfer}$

1918 J. Perrin proposed the mechanism of resonance energy transfer. A theoretical interpretation of energy transfer between molecules, involved fluorescence polarization in a solution of a single chemical species of fluorophore.

1922 G. Cario and J. Franck demonstrate that excitation of a mixture of mercury and thallium atomic vapors with 254nm (the mercury resonance line) also displayed thallium (sensitized) emission at 535nm.

1928 H. Kallmann and F. London developed the quantum theory of resonance energy transfer between various atoms in the gas phase. The dipole-dipole interaction and the parameter $R_{\rm O}$ were used for the first time.

1932 F. Perrin published a quantum mechanical theory of energy transfer between molecules of the same specie in solution. Qualitative discussion of the effect of the spectral overlap between the emission spectrum of the donor and the absorption spectrum of the acceptor.

1941 W. Arnold and J.R. Oppenheimer, an abstract on FRET in photosynthesis and full article in 1950 $\,$

1946-1949 T. Förster developed the first quantitative theory of molecular resonance energy transfer.

History singlet-singlet energy transfer

Hg vapor to Na vapor

G. Cario and J. Franck, Z. Physik, 17, 202 (1923).

 $Hg \ vapor \ to \ H_2$

Xe vapor to H₂

H. Calvert, Z. Physik, 78, 479 (1932)

Anthracene to Naphthalene crystals

A. Winterstein and K. Schon, Naturwiss., 22, 237 (1934)

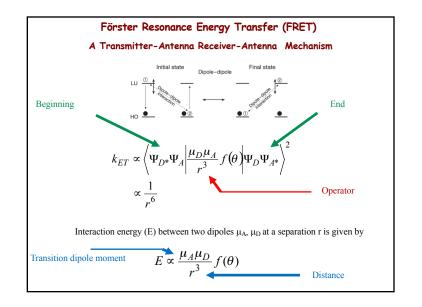
E. J. Bowen, Nature, 142, 108 (1938)

Tryptaflavin to Rhodamine B in solution (> 70Å)

T. Forster, Z. Elektrochem., 63, 93 (1949)

1-Chloroanthracene to perylene

E. Bowen and B. Brocklehurst, Trans. Faraday Soc., 49,1131 (1953)

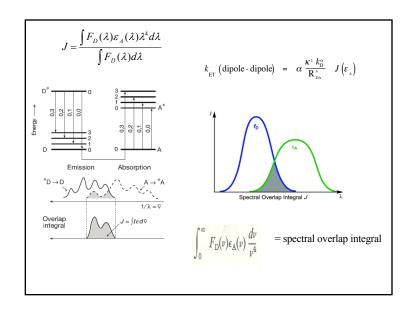


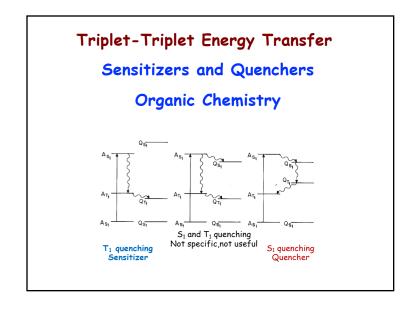
$$\Delta E (*D \to D) = \Delta E (A \to *A)$$

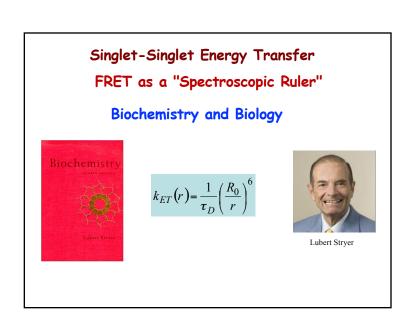
$$E \propto \frac{\mu_A \mu_D}{r^3} f(\theta) \qquad \text{Operator}$$

$$k_{\text{ET}} (\text{dipole-dipole}) \rightarrow \frac{k_D^o \int \varepsilon_A}{R_{DA}^6}$$

$$k_{\text{ET}} (\text{dipole-dipole}) = \alpha \frac{\kappa^2 k_D^o}{R_{DA}^6} J(\varepsilon_A)$$







Förster formulation

$$k_{ET}(r) = \frac{1}{\tau_D} \left(\frac{R_0}{r}\right)^6$$

$$k_{ET} = \frac{\phi_D \kappa^2}{\tau_D r^6} \frac{9000 \ln 10}{128\pi^5 N_A n^4} \int_0^\infty F_D(\lambda) \epsilon_A(\lambda) \lambda^4 d\lambda$$

 ϕ_D : Fluorescence quantum yield of donor in absence of acceptor

κ²: Orientation factor

 τ_D : Lifetime of donor in absence of acceptor

r: Donor - acceptor distance

N_A: Avogadro number

n : Refractive index of the medium

 $F_D(\lambda)$: Normalized fluorescence spectrum of donor

 $\varepsilon_{A}(\lambda)$: Normalized absorption spectrum of acceptor

Definition of Ro



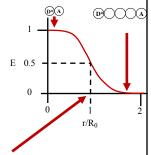


А

In the absence of acceptor: $k[D^*]$

In the presence of acceptor: $k[D^*] + k_{ET} [D^*][A]$

We make an assumption that when $r = R_0$ $k[D^*] = k_{ET} [D^*][A]$



At $r_{DA} = R_{DA}$:

The deactivation of excited state would be $k_{ET}[D^*] + k[D^*][A] = 2 k[D^*]$

What happens to Förster formulation at R_0

$$k_{ET} = \frac{\phi_D \kappa^2}{\tau_D r^6} \frac{9000 \ln 10}{128\pi^5 N_A n^4} \int_0^\infty F_D(\lambda) \xi_A(\lambda) \lambda^4 d\lambda$$

When $r = R_o$ the rate of energy transfer equals the rate of deactivation.

$$k_{ET} = k_{D} = \tau_{D}^{-1}$$

$$\mathbf{T}_{D}^{*1} \quad \mathbf{K}_{ST} = \frac{\phi_{D} \kappa^{2}}{\tau_{D} \rho^{6}} \frac{9000 \ln 10}{128 \pi^{5} N_{A} n^{4}} \int_{0}^{\kappa} F_{D}(\lambda) \hat{\mathbf{x}}_{A}(\lambda) \lambda^{4} d\lambda$$

Replacing r with R_0 and rearranging the above eqn.

$$R_{0^{6}} = \frac{\phi_{D}\kappa^{2}}{128\pi^{5}N_{A}n^{4}} \int_{0}^{\infty} F_{D}(\lambda) k_{A}(\lambda) \lambda^{4} d\lambda$$

R₀ can be calculated using this eqn.

For each D-A pair the # is fixed

$$k_{ET} = \frac{1}{\tau_D r^6} \frac{\phi_D \kappa^2}{1} \frac{9000 \ln 10}{128\pi^5 N_A n^4} \int_0^\infty F_D(\lambda) \epsilon_A(\lambda) \lambda^4 d\lambda$$

$$R_0^6 = \frac{\phi_D \kappa^2}{28\pi^5 N_A n^4} \int_0^\infty F_D(\lambda) \epsilon_A(\lambda) \lambda^4 d\lambda$$

$$k_{ET}(r) = \frac{1}{\tau_D} \left(\frac{R_0}{r}\right)^6$$

 $\mathbf{R}_0 = \mathbf{Forster} \ \mathbf{distance}$

 R_0 is constant for a particular donor – acceptor pair in a given solvent

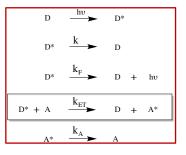
What one needs to estimate 'r'?

$$k_{ET}(r) = \frac{1}{\tau_D} \left(\frac{R_0}{r}\right)^6$$

One can get 'r', if we can measure

- k_{ET} (Rate constant of energy transfer)
- τ_D (Lifetime of donor in absence of acceptor)
- R₀ is calculated.

What is k_{ET}



Follow the fluorescence of the donor

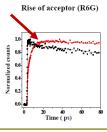
$$\Phi^{F} = \frac{k_{F}}{k_{F} + k}$$

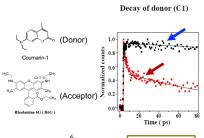
$$\Phi_{A^F} = \frac{k_F}{k_F + k + k_E}$$

$$\frac{\Phi_{F}}{\Phi_{A}^{F}} = \frac{k_{F} + k + k_{ET}}{k_{F}} x \frac{k_{F}}{k_{F} + k}$$

$$\frac{\Phi_{F}}{\Phi_{A}^{F}} = 1 + \frac{k_{ET}}{k_{F} + k} = 1 + \tau k_{ET}$$







Inverse rise time of acceptor fluorescence is: k_{ET}

$$k_{ET} = \frac{1}{\tau_D} \left(\frac{R_0}{r}\right)^6$$

k	_ 1_	1
κ_{ET}	τ_{DA}	$ au_D$

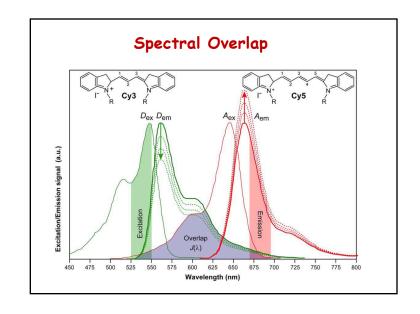
System	$ au_{ m rise}^{ m A}$	$\tau_D^{\ 0}$	$\mathbf{R_0}$	R_{DA}
C480@OA ₂ +R6G	1.5 ps	4900 ps	48.8 Å	13±1 Å
C153@OA ₂ +R6G	1.0 ps	7400 ps	55.7 Å	13±1 Å
C1@OA ₂ +R6G	3.5 ps	4300 ps	42.5 Å	13±1 Å

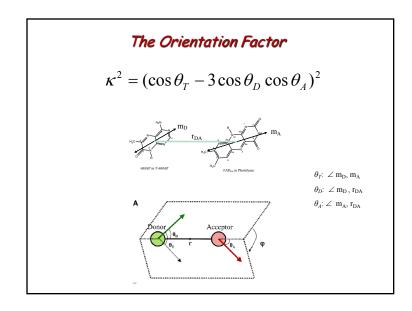
Förster radius - examples

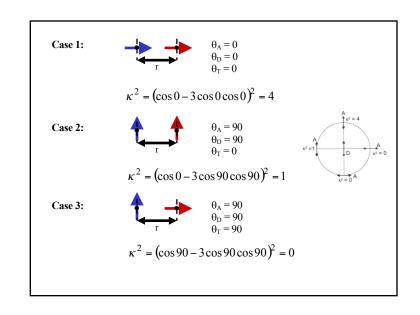
Some typical donor-acceptor pairs commonly used in structural mapping of proteins, and their values of R_0 :

Donor	Acceptor	R_0 [Å]
Fluorescein HO	Tetmethylrhodamine	55
$\begin{array}{c} \text{IAEDANS} & \overset{\text{o}}{\underset{\text{SO_3H}}{\text{H-Ch}_2\text{Ch}_2\text{NH-C}^1-\text{Ch}_2\text{I}}} \end{array}$	Fluorescein	46
Tryptophan	DPH (CH=CH) ₃	40
Fluorescein	Fluorescein	44
BODIPY	BODIPY	57

	$\frac{9000 \ln 10}{28\pi^5 N_A n^4} \int_0^\infty F_D(\lambda) A(\lambda) \lambda^4 d\lambda$	
Tab. 9.1. Examples of Förster critical Donor	Acceptor Acceptor	Ro (A
Naphthalene	Dansyl	~22
Anthracene	Perylene	~31
Pyrene	Perylene	~36
Phenanthrene	Rhodamine B	~47
Fluorescein	Tetramethylrhodamine	~55
Fluorescein-5-isothiocyanate	Eosin maleimide	~60
Rhodamine 6G	Malachite green	~61
Tryptophan	Dansyl	~21
Tryptophan	ANS	~23
Tryptophan	Anthroyl	~25
Tryptophan	Pyrene	~28







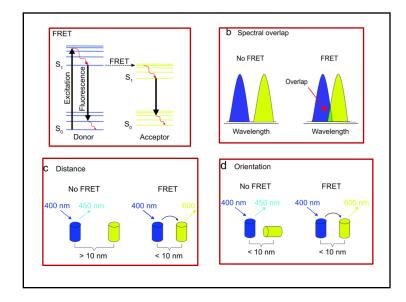
Case 4:

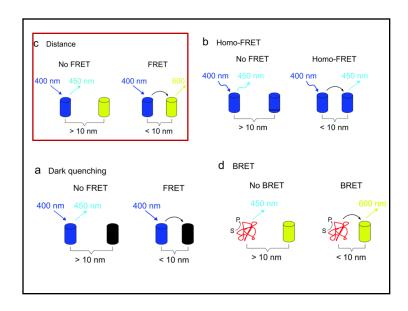
When the transition moment of donor and acceptor are normalized The value of κ^2 can be taken as an average

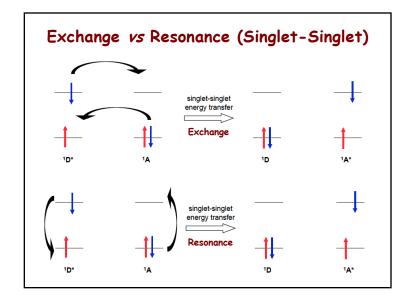
$$\left\langle \kappa^2 \right\rangle = \frac{\int\limits_0^\pi \left(\cos\theta_T - 3\cos\theta_D\cos\theta_A\right)^2 d\theta_T d\theta_D d\theta_A}{\int\limits_0^\pi d\theta_T d\theta_D d\theta_A} = \frac{2}{3}$$

The rate of energy transfer between a donor and acceptor is given by where k is taken to be 2/3; this is an assumption, need not be true all the time.

$$k_{ET} = \frac{1}{\tau_D r^6} \frac{\phi_D \kappa^2}{1} \frac{9000 \ln 10}{128 \pi^5 N_A n^4} \int_0^\infty F_D(\lambda) \chi_A(\lambda) \lambda^4 d\lambda$$





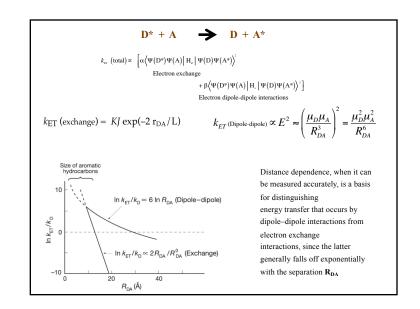


Differences between Förster (dipole-dipole interaction) and Dexter (electron exchange) energy transfer processes

- The rate of dipole-induced energy transfer decreases as R⁻⁶ whereas
 the rate of exchange-induced transfer decreases as e-(2r/L).
 Quantitatively, this means that k_{ET} (exchange) drops to negligibly
 small values (relative to the donor lifetime) as the intermolecular
 (edge-to-edge) distance increases more than on the order of one or
 two molecular diameters (5-10Å)
- The rate of dipole-induced transfer depends on the oscillator strength of the *D → D and A → *A radiative transitions, but the rate of the exchange-induced transfer is independent of the oscillator strength of the *D → D and A → *A transitions

Dipole-dipole mechanism will be most favored for *D and A pairs such that:

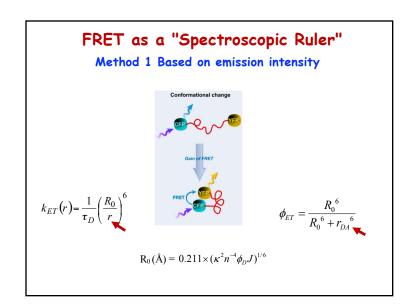
- The *D \rightarrow D and A \rightarrow *A processes correspond to a large (spectral) overlap integral, *J*.
- The radiative rate constant, k° D, is as large as possible.
- \bullet The magnitude of ϵ_A is as large as possible.
- \bullet There is a small spatial separation between *D and A.
- There will be a preferred orientation for which energy transfer is most favorable.

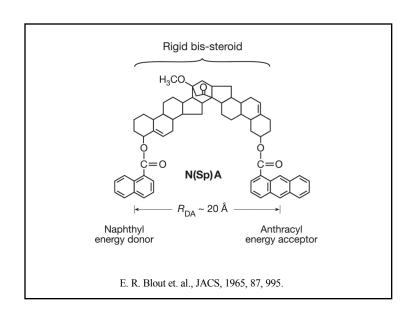




A Theory of Sensitized Luminescence in Solids, D. L. Dexter, J. Chem. Phys. 21, 836 (1953)

Transfer mechanisms of electronic excitation, Th. Forster, Discussions Faraday Soc. 27, 7, (1959)





Experimental verification of Förster formulation

An Experimental Study of the Transfer of Energy of Excitation between Unlike ${\bf Molecules~in~Liquid~Solutions^{1}}$

By Edmund J. Bowen and Robert Livingston

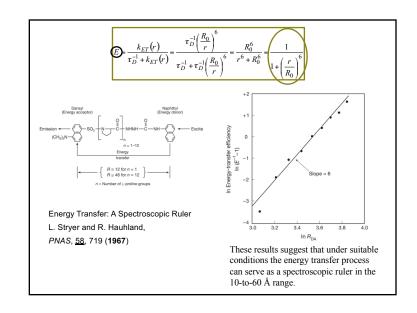
J. Am. Chem. Soc, 76, 6300, 1954

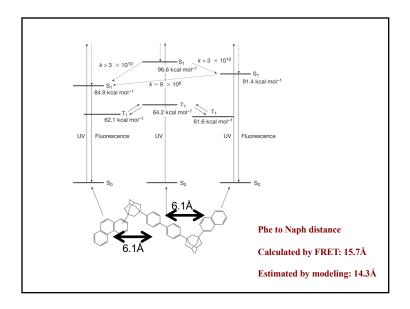
SUMMARY OF THE RATE CONSTANTS AND RELATED QUANTITIES						
A B Solvent	Chloroanthracene perylene benzene	Chloroanthracene perylene chloroform	Chloroanthracene perylene liquid paraffin	Chloroanthracene rubrene benzene	Cyanoanthracene rubrene benzene	
R1/2, Å.	41	(42)	(39)	38(?)	84	

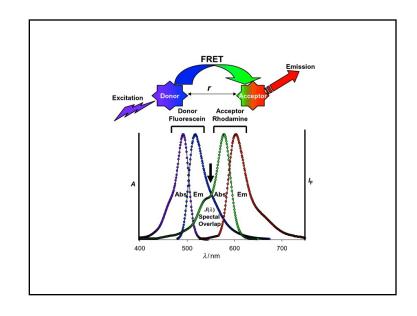
An Experimental Study of Energy Transfer between Unlike Molecules in Solution

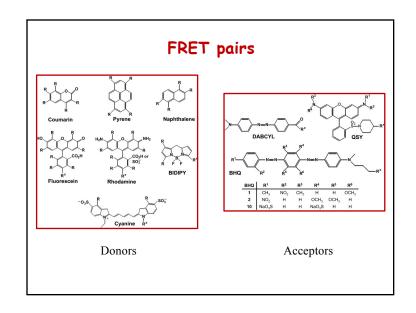
By WILLIAM R. WARE J. Am. Chem. Soc, 83, 4374, 1961

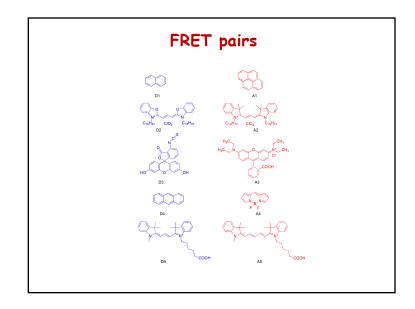
Pair	k_{i} (exp.), M ⁻¹ sec. ⁻¹	R ₀ , Å. (th.)	R ₀ , Å. (exp.)
Anthracene*-perylene	1.2×10^{11}	31	54
Perylene*-rubrene	1.3×10^{11}	38	65
9,10-Dichloroanthracene*-perylene	8.0×10^{10}	40	67
Anthracene*-rubrene	3.7×10^{10}	23	39
9,10-Dichloroanthracene*-rubrene	3.1×10^{10}	32	49

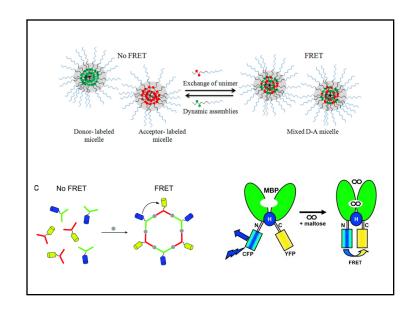


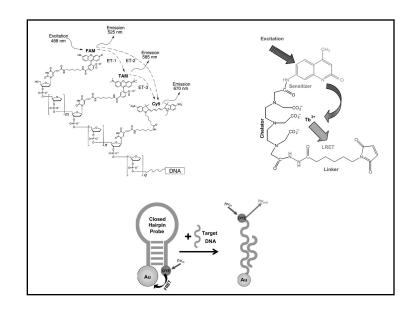


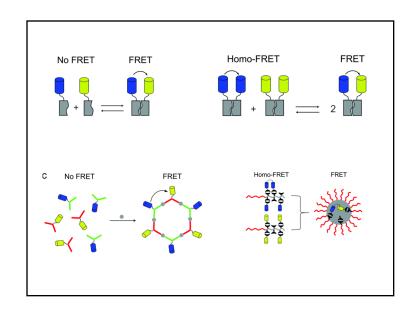


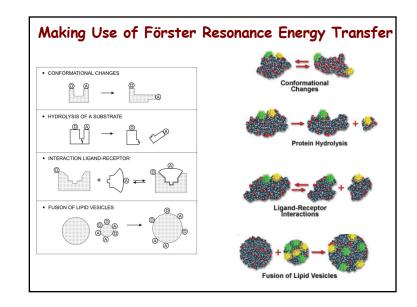


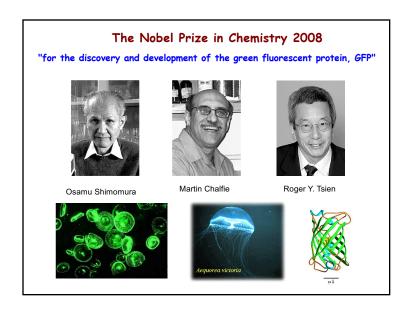


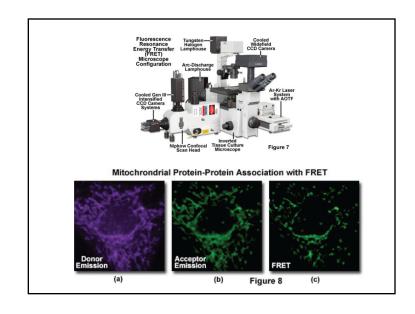


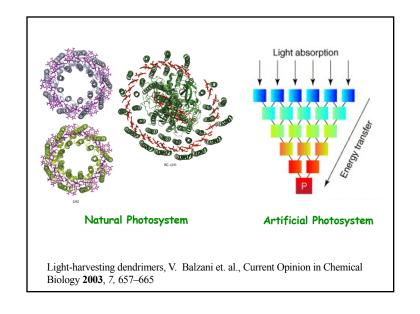


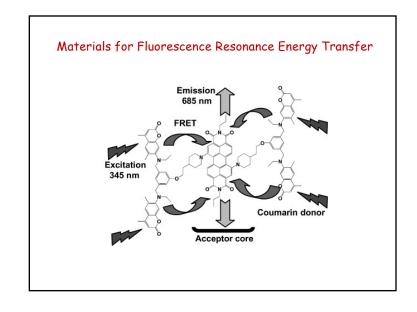


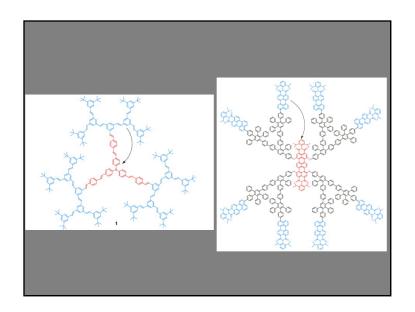


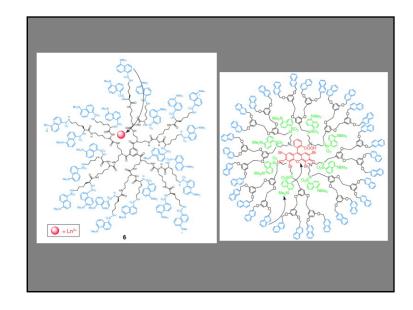


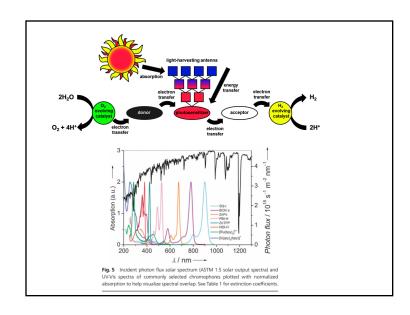


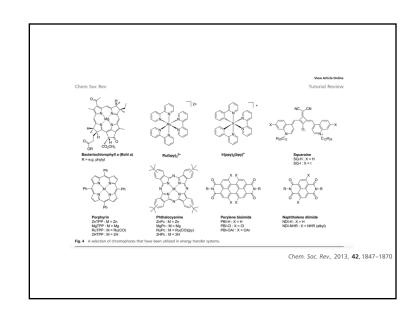


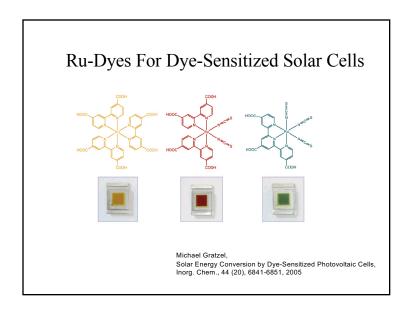


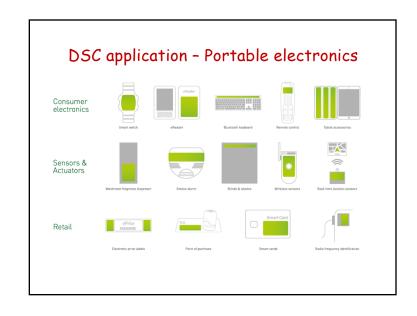


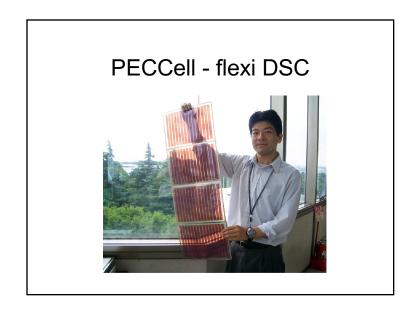


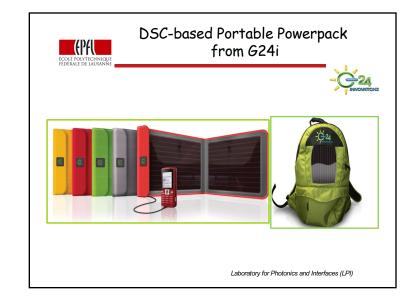






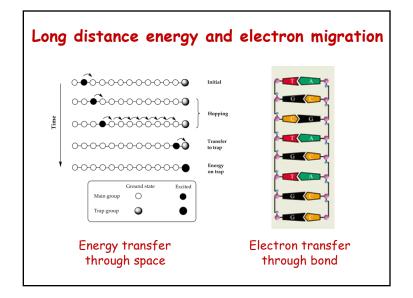






Large area DSC panels for outdoor and building integration





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